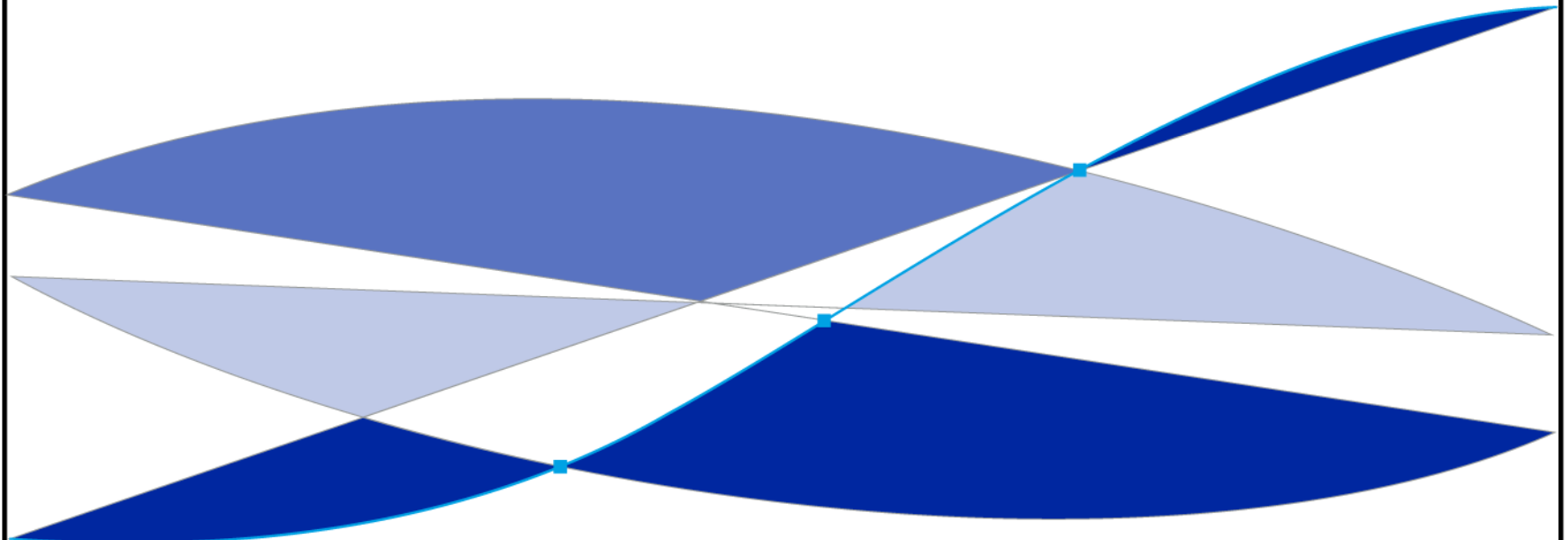


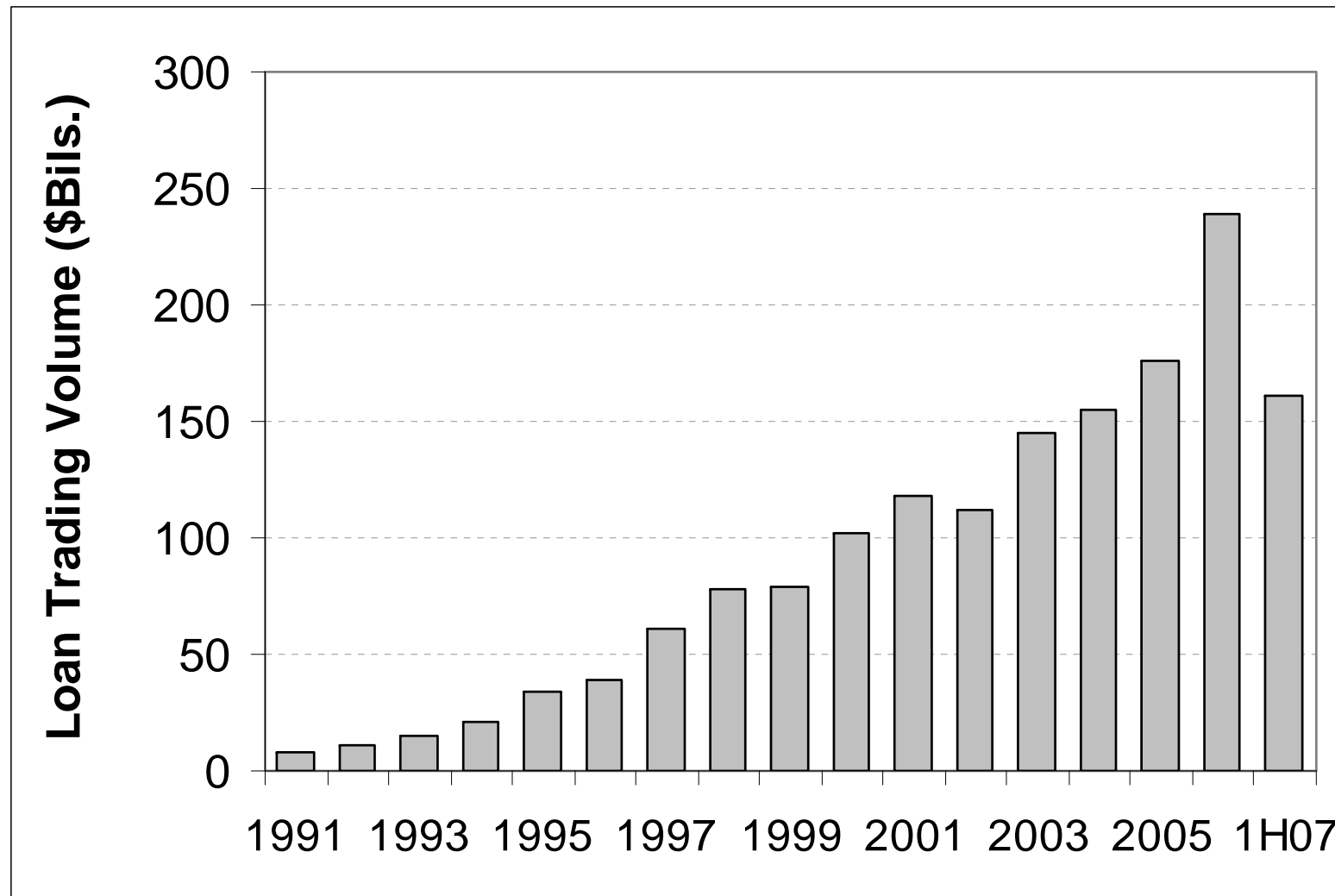
Navigating Cash Loan and LCDS Markets



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Trading Volume in the U.S. Syndicated Loan Market



Agenda

- 1. Prepayment Option and Lattice Valuation**
- 2. Prepayment Pattern and Expected Life**
- 3. Option Adjusted Spread and Par Spread**
- 4. How Cancelable are LCDS Contracts?**
- 5. Duration and Convexity**
- 6. Summary**

1

Prepayment Option and Lattice Valuation Methodology

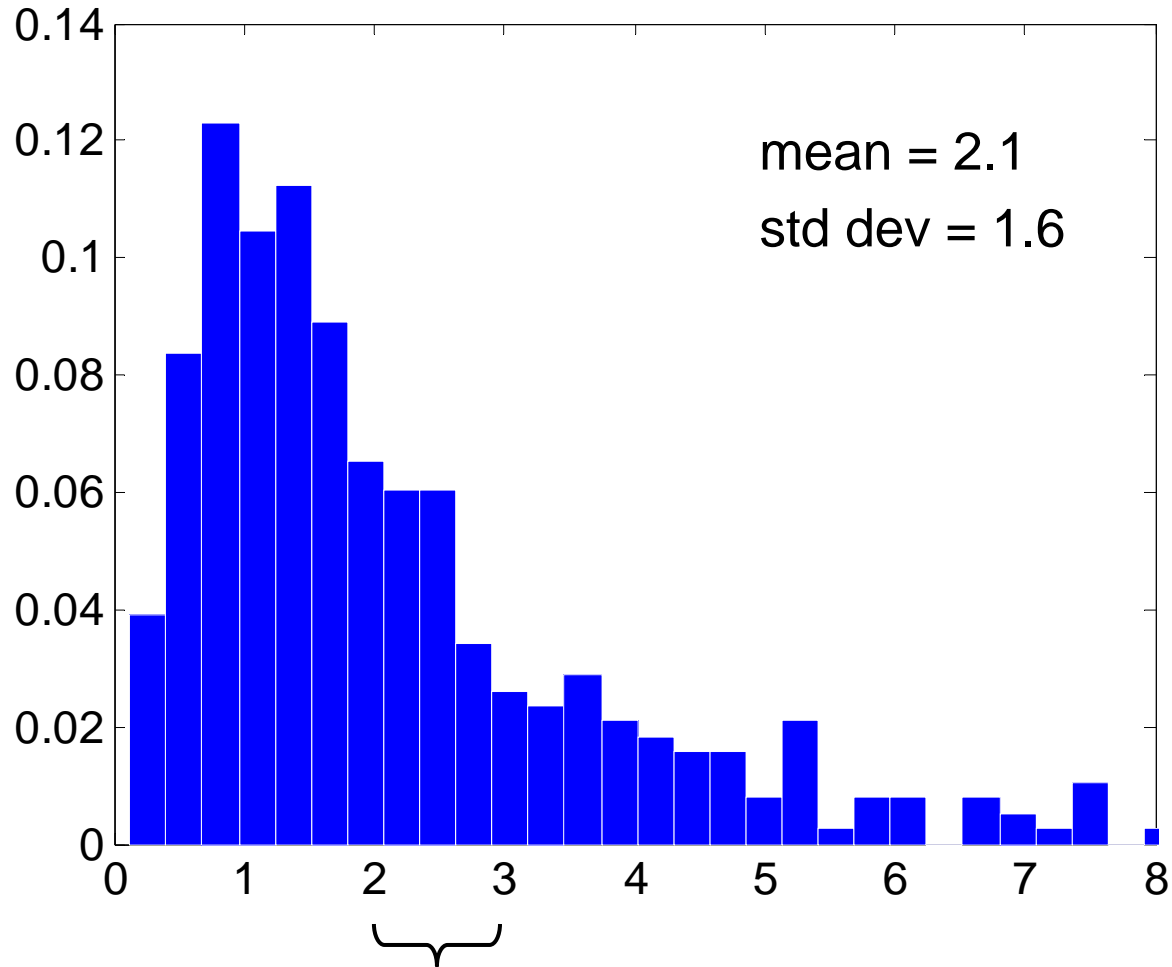
Prepayment Option and Credit Spread

- Most Loans are prepayable, often with friction. Investors want to obtain a pure credit spread measure on loans.
- Loan traders often take a back-of-envelope approach by assuming or estimating a shortened loan maturity between 2 to 3 years, say 2.5 years.
- They then try to back out the credit spread based on market price:

$$\text{Market Price} = \sum_{t>0}^{2.5} \frac{CF_t}{\left(1 + r_t^{\text{RiskFree}} + s\right)^t}$$

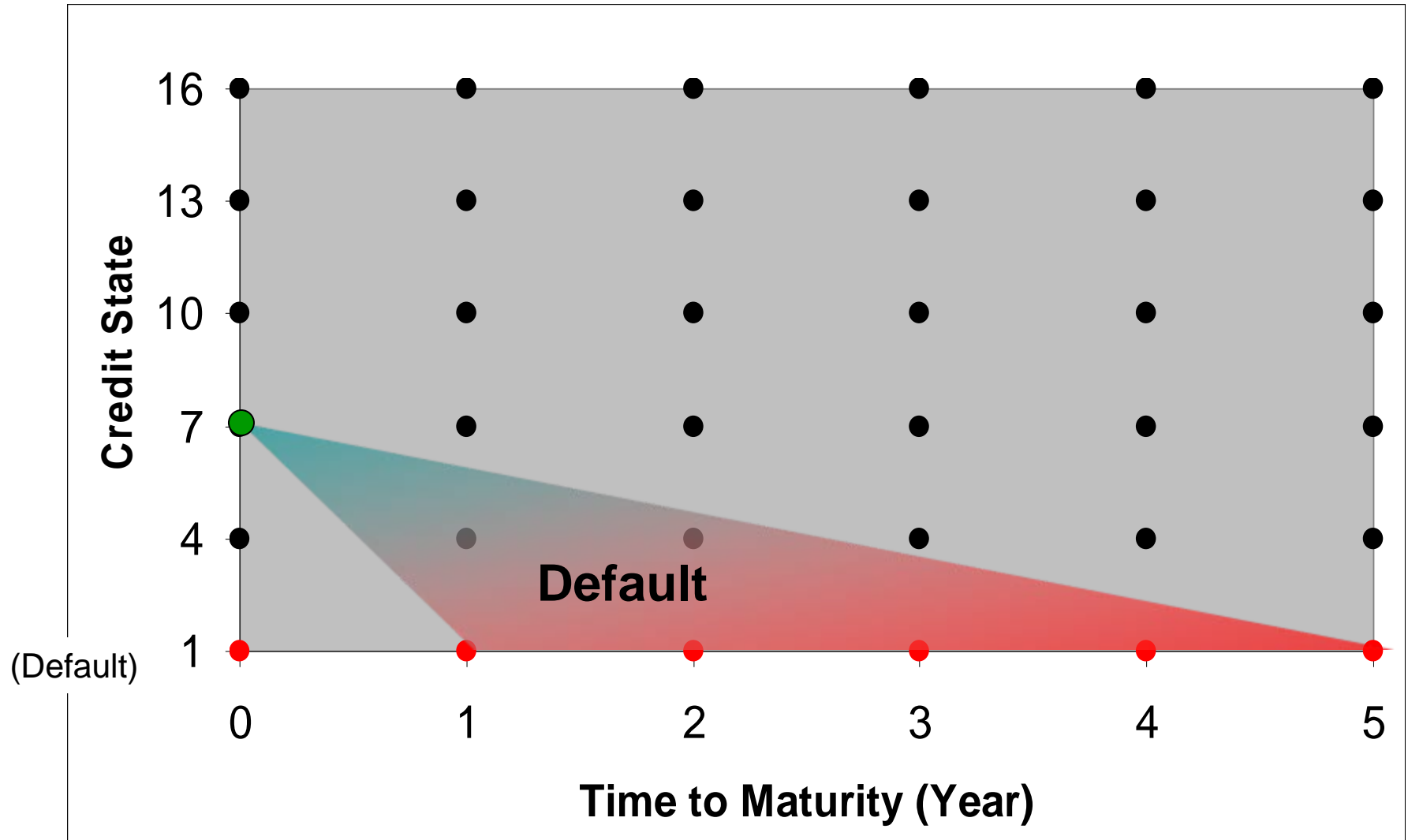
- Problems with this simplistic approach...

Actual Time from Origination to Prepayment

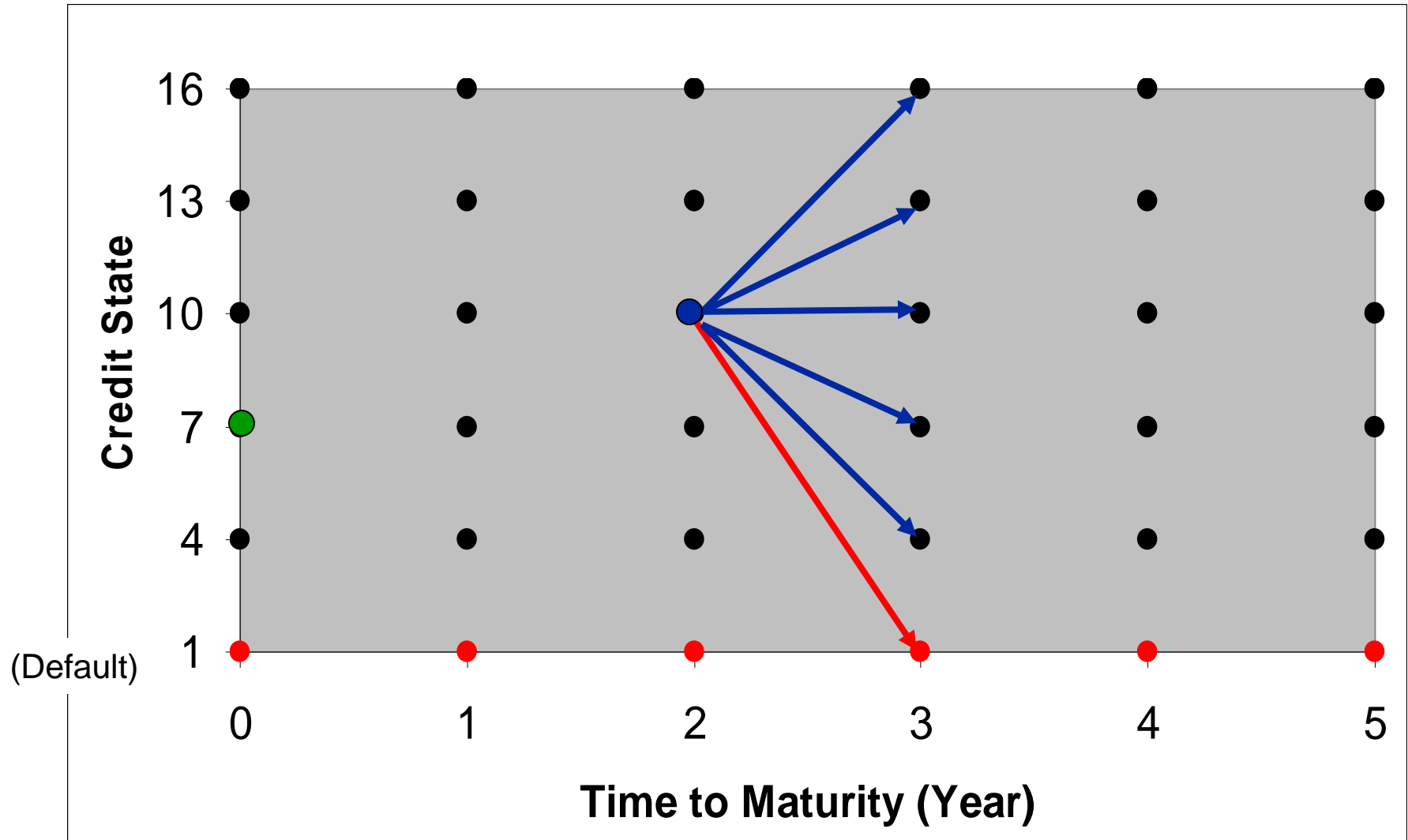


$$\Pr \{ 2 \leq t_{pp} \leq 3 \mid \text{Prepay} \} = 17.3\%$$

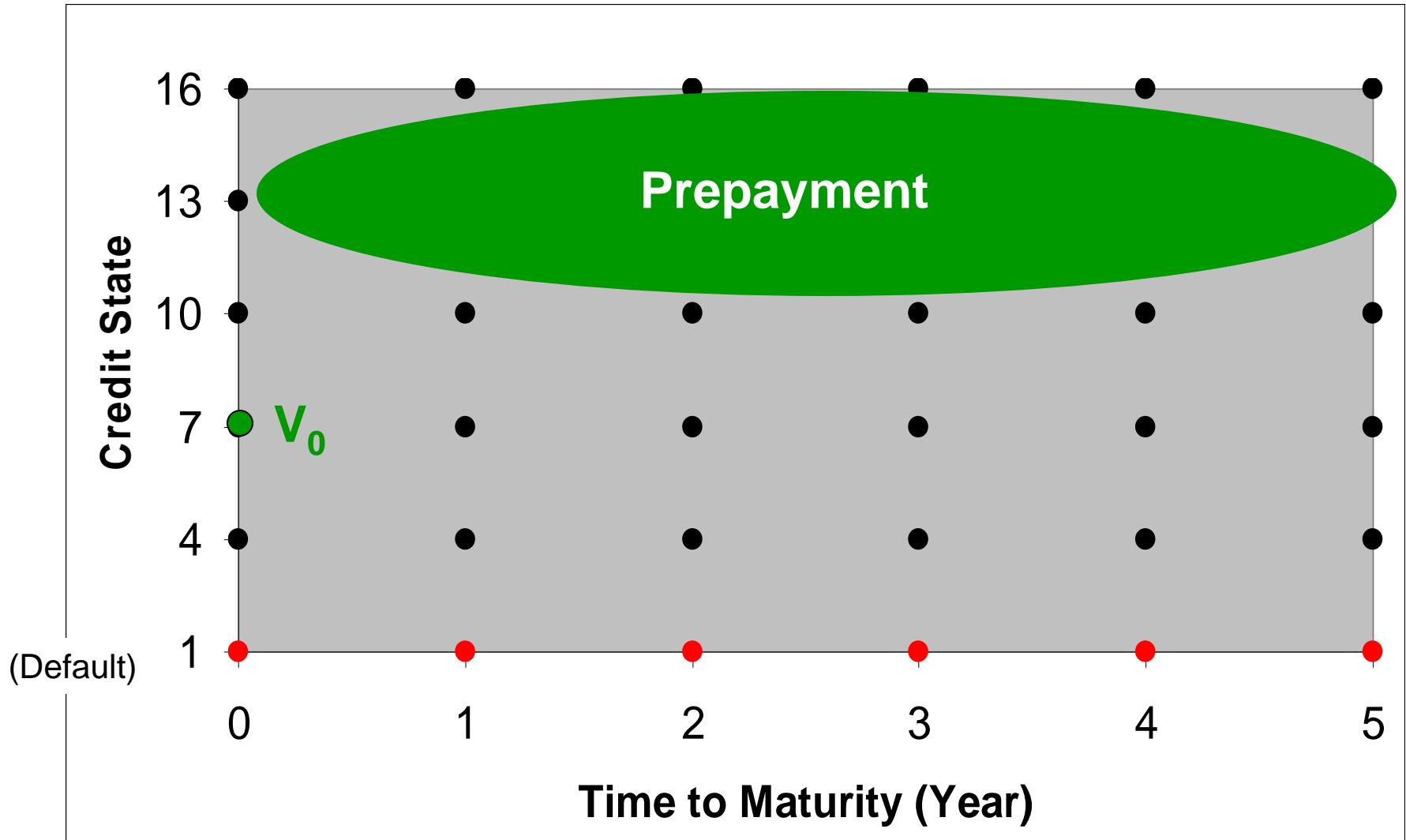
Moody's KMV Lattice Valuation Model



Credit Migration



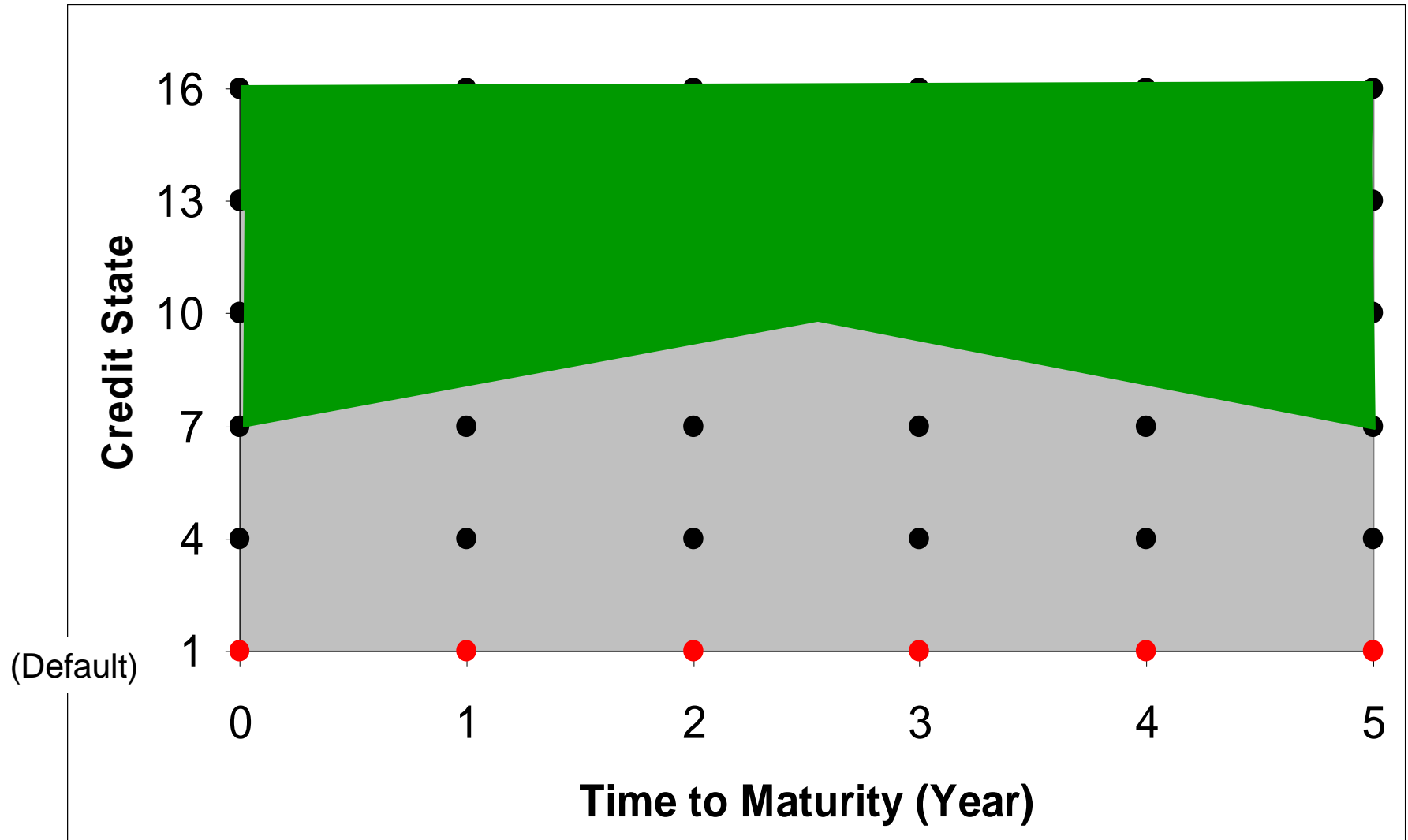
Results From Lattice Valuation



2

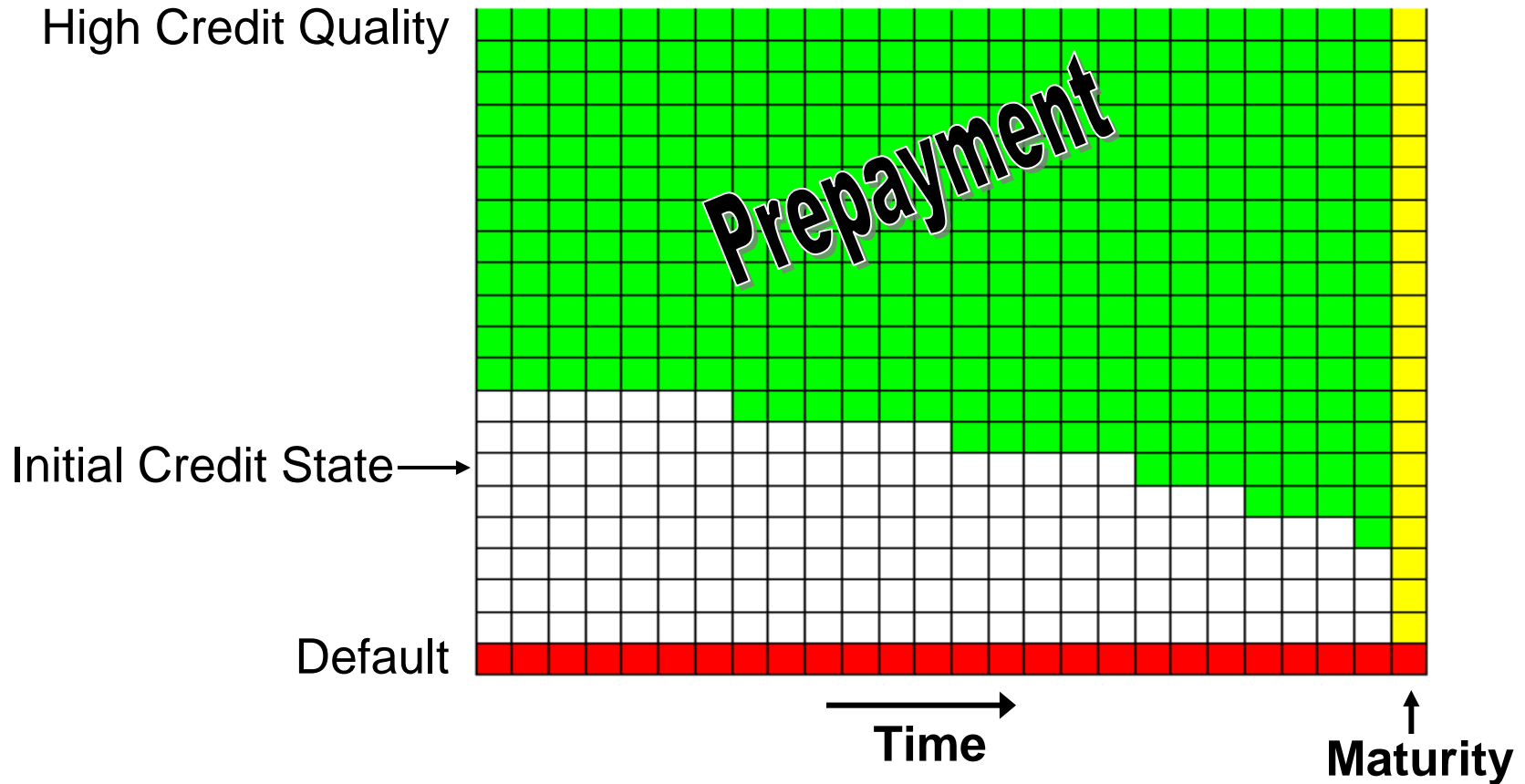
Prepayment Pattern and Expected Life

Pattern?



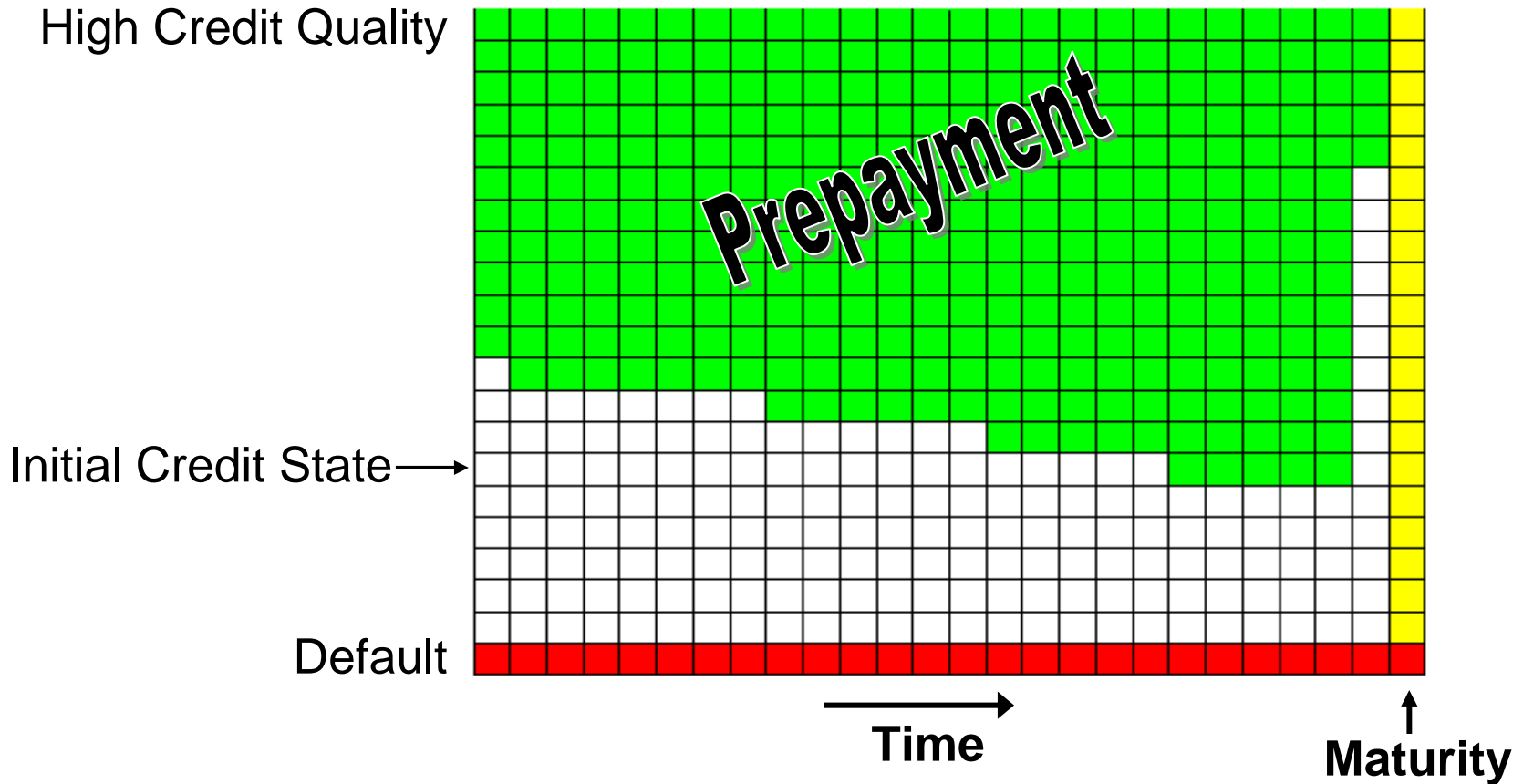
Prepayment Decision over time

Prepayment friction: **none**



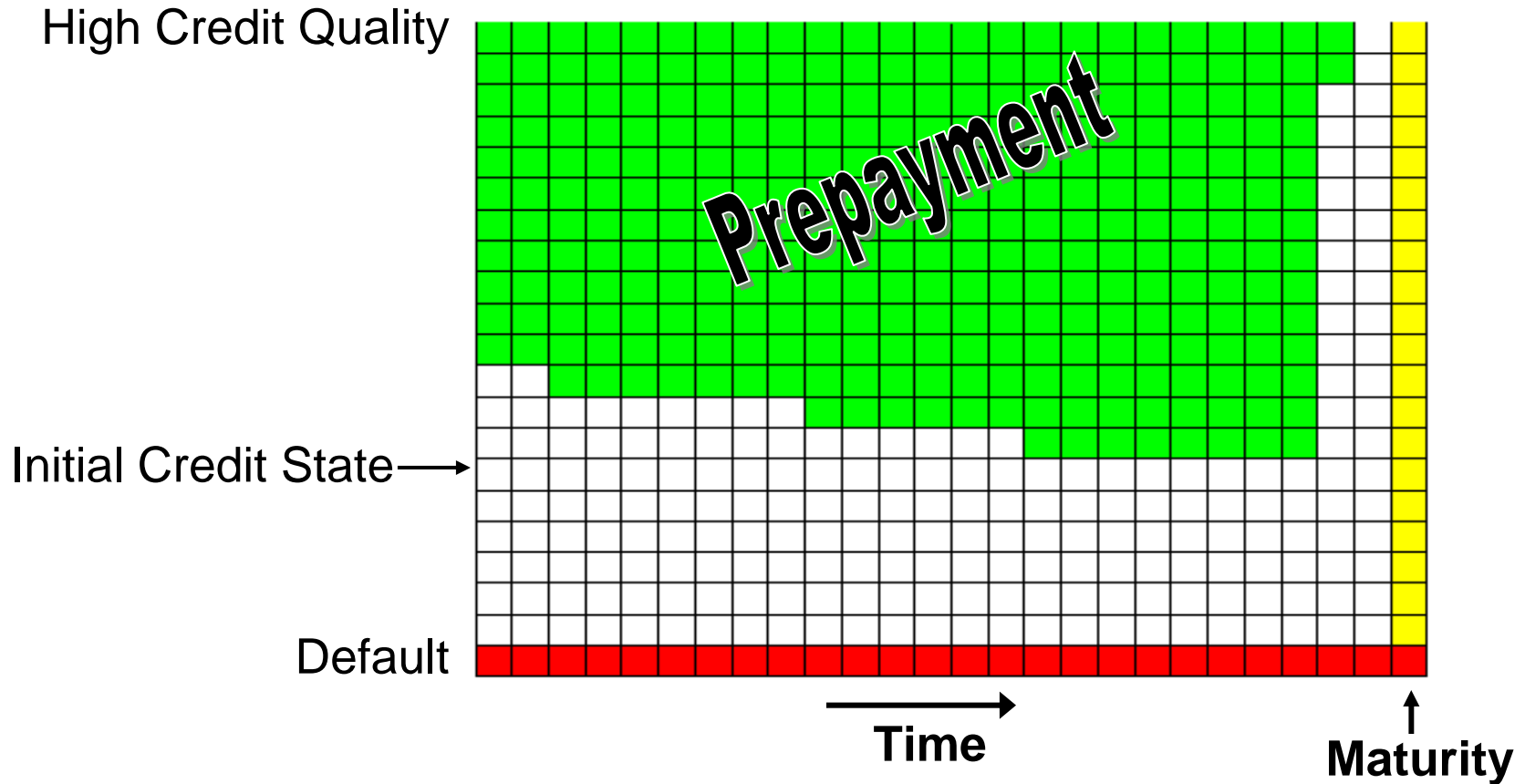
Prepayment Decision over time

Prepayment friction: 50 bps



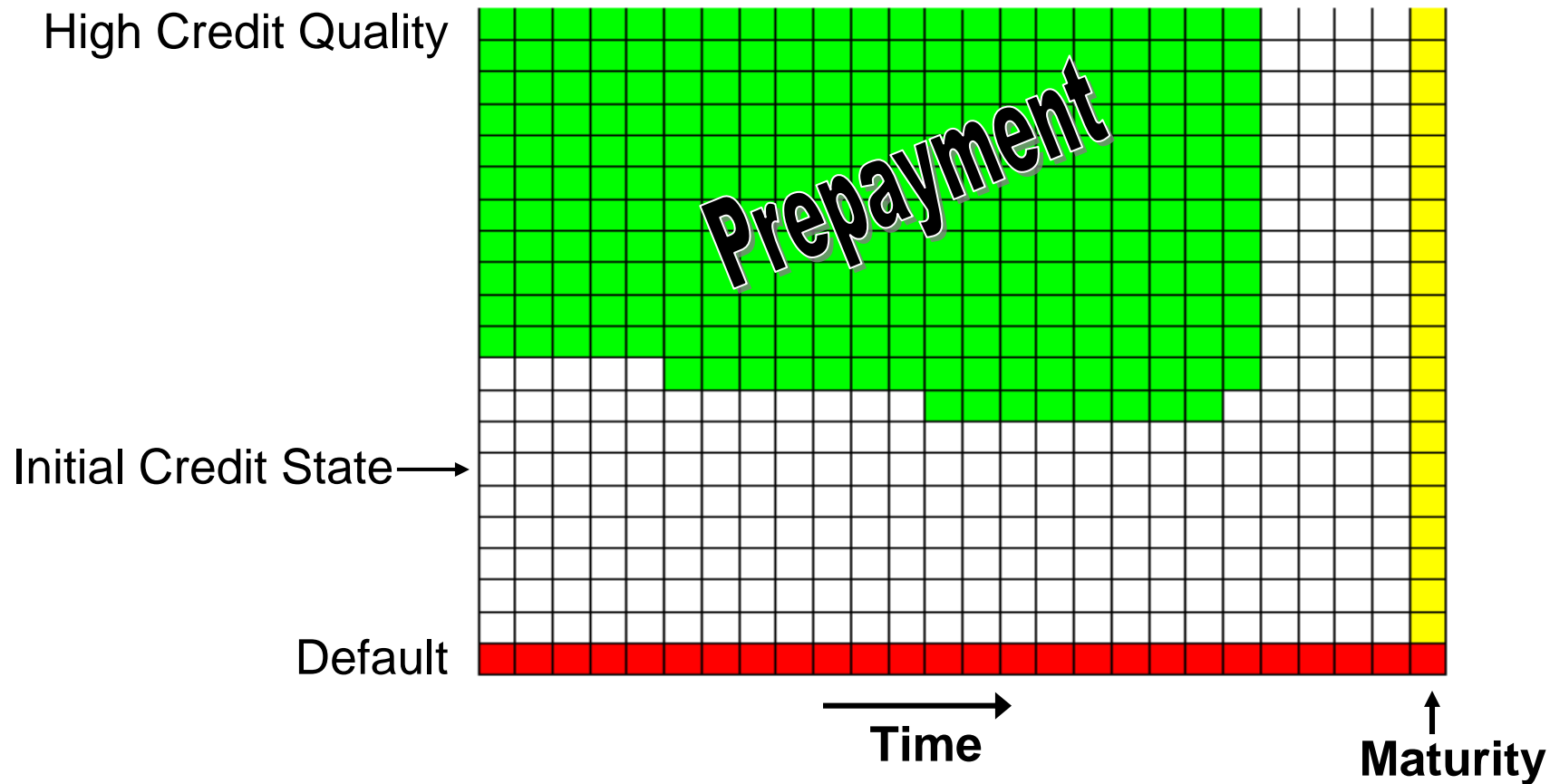
Prepayment Decision over time

Prepayment friction: 100 bps



Prepayment Decision over time

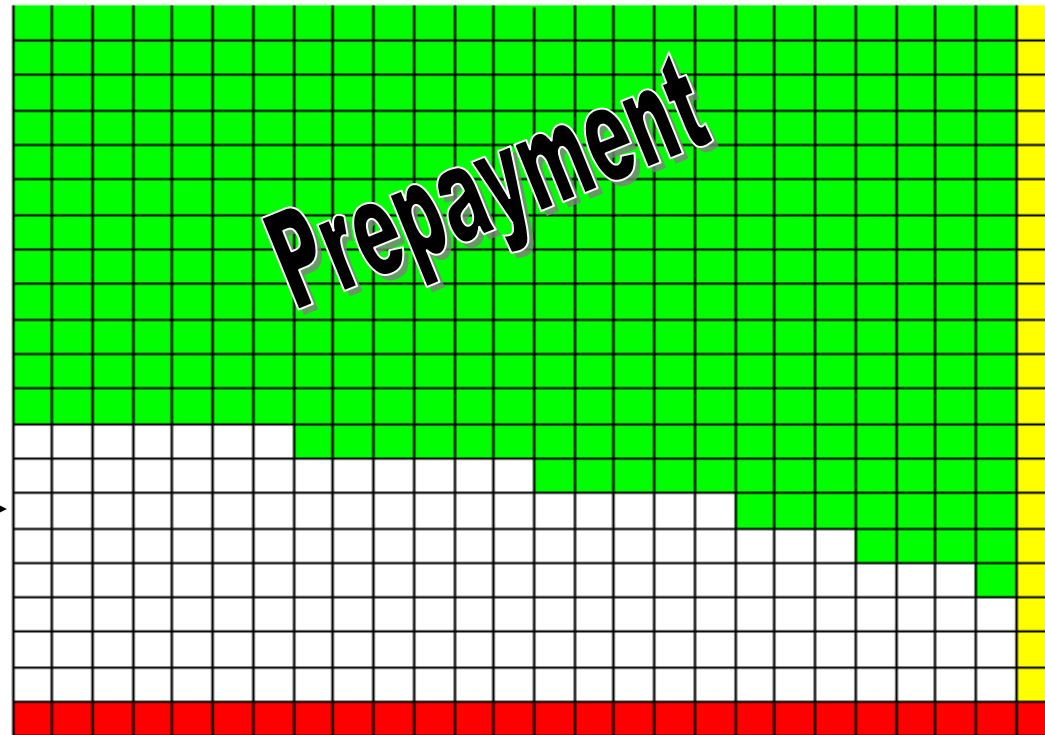
Prepayment friction: **200 bps**



Early Termination Probabilities

Prepayment friction: **none**

High Credit Quality

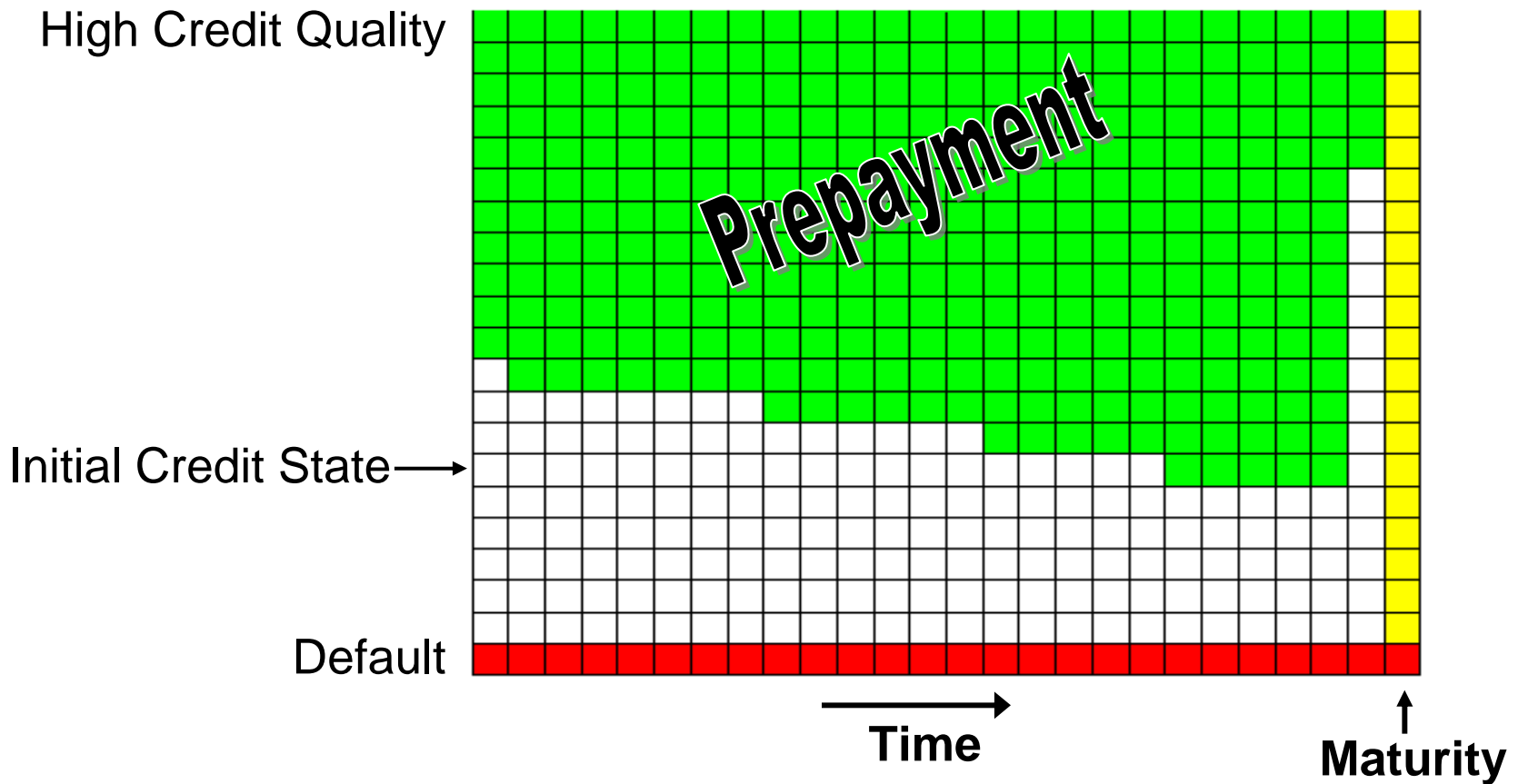


$$\begin{array}{ccccccc}
 \uparrow & & \uparrow & & & & \uparrow \\
 7.7\% & & 4.7\% & & & & 1.5\% \\
 \times & + & \times & + & + & \dots & \times \\
 0.67 & & 1.92 & & & & 5.67
 \end{array}$$

Expected Life = 2.8 years

Expected Life

Prepayment friction: **50 bps**, **Expected Life = 2.9 years**



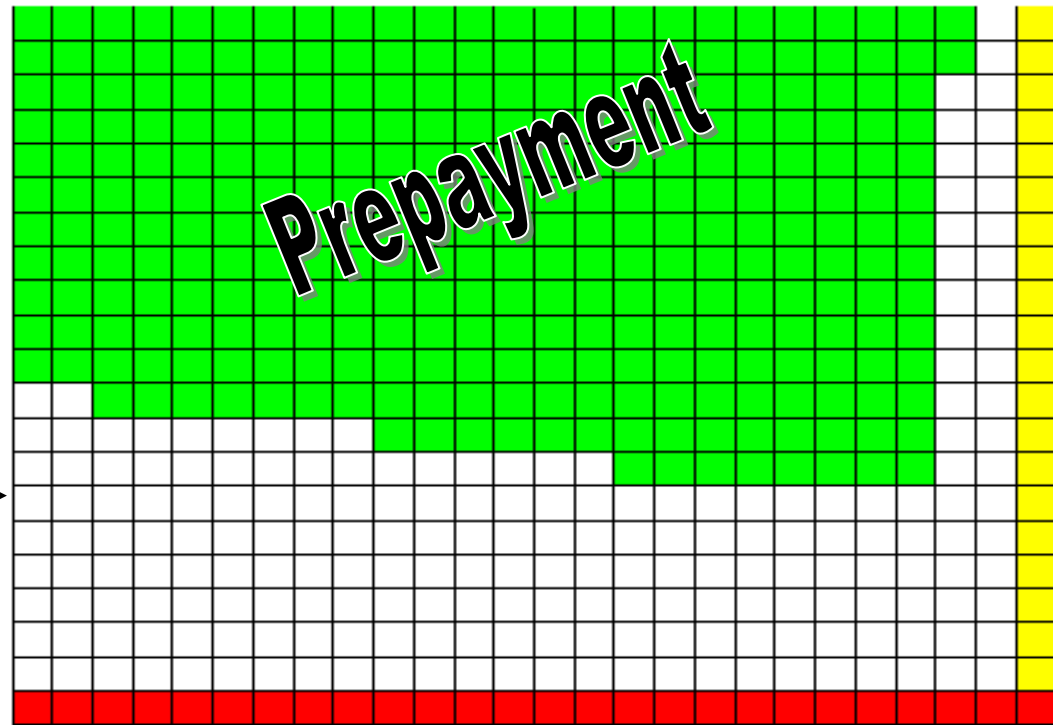
Expected Life

Prepayment friction: **100 bps**, **Expected Life = 3.0 years**

High Credit Quality

Initial Credit State →

Default

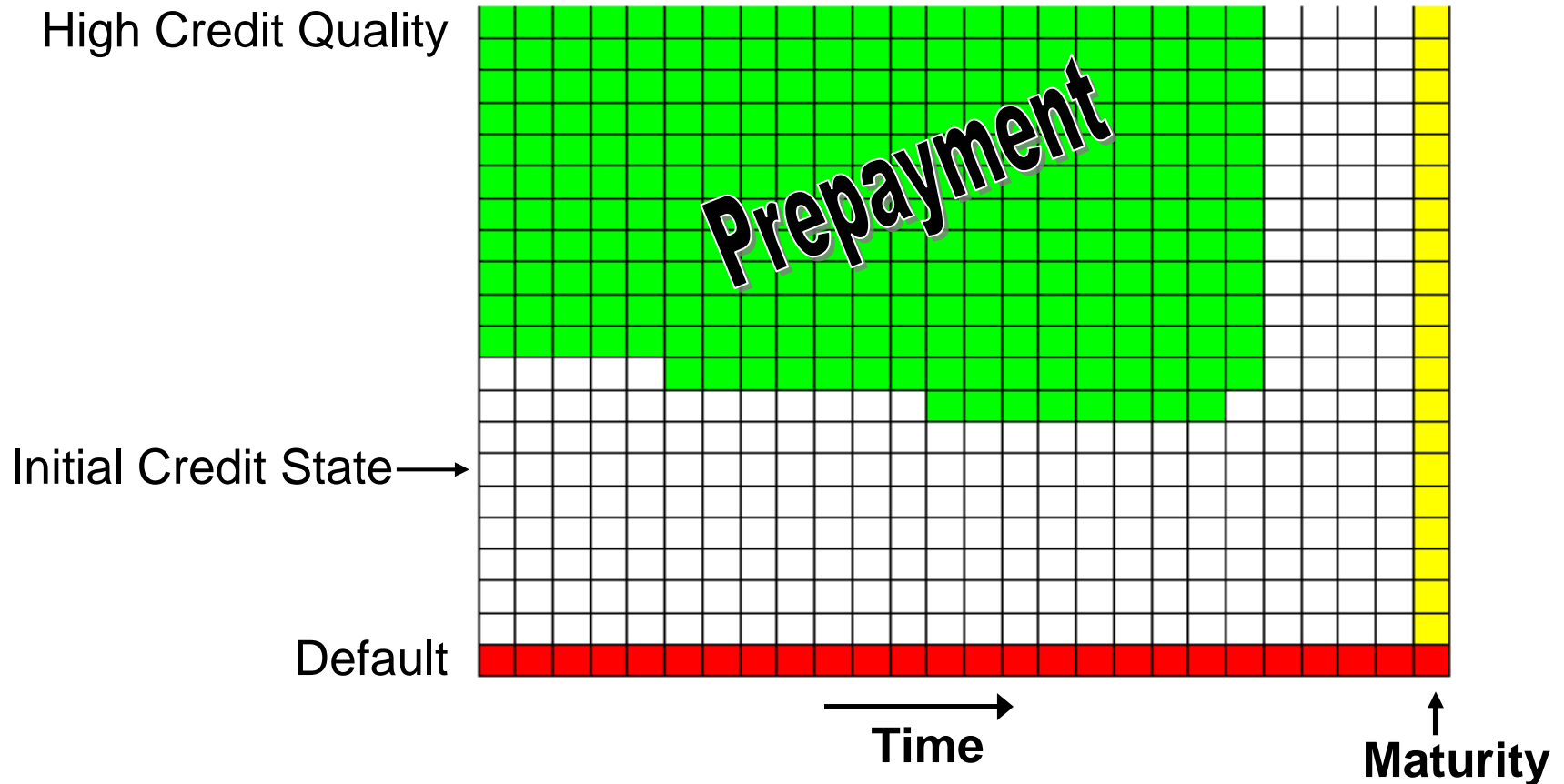


Time →

↑ Maturity

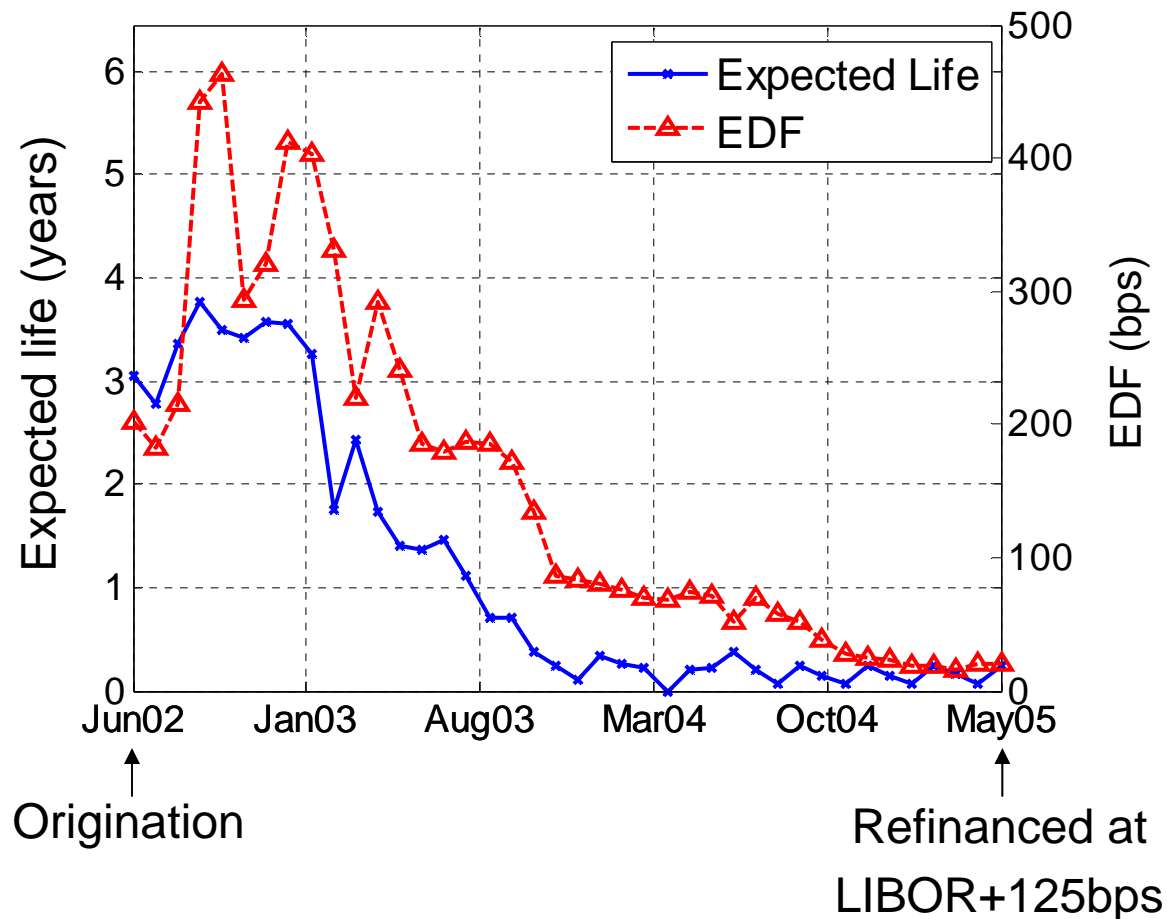
Prepayment Decision over time

Prepayment friction: **200 bps**, **Expected Life = 3.4 years**



Expected Life Example

- Silgan Holdings Inc, bullet term loan, B1 senior unsecured
- 6.5yr tenor @ LIBOR+200bps



3

Option Adjusted Spread and Par Spread

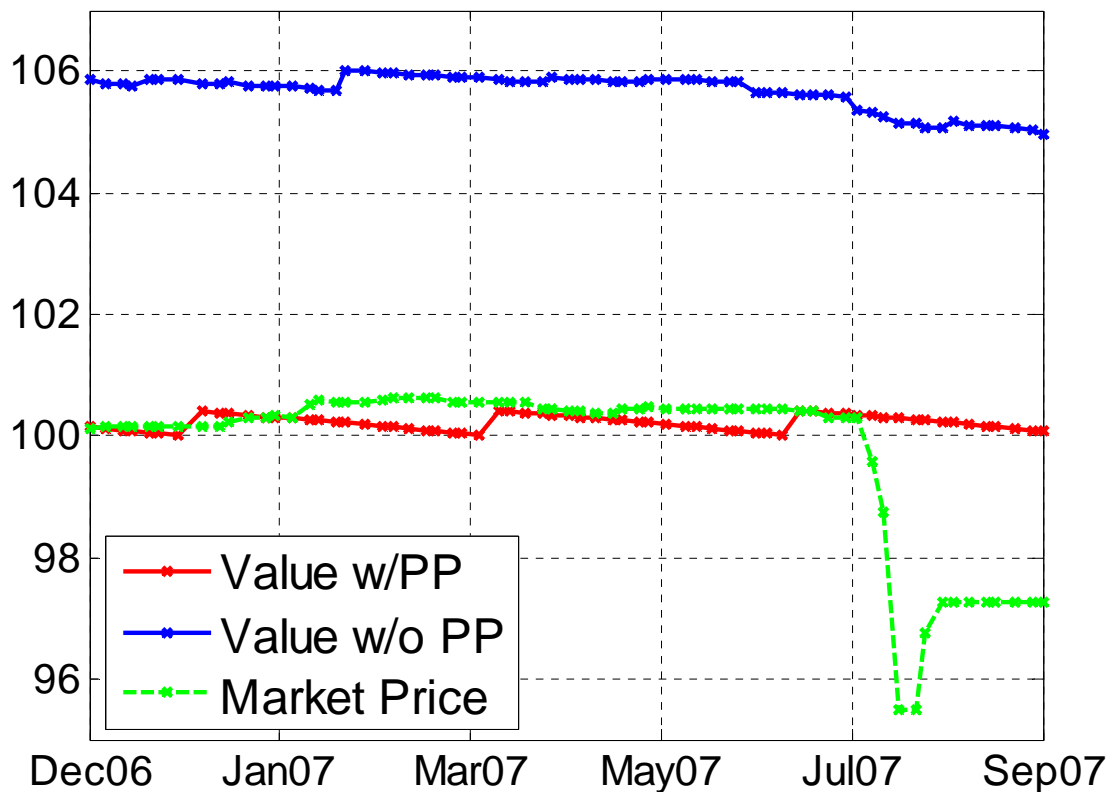
Loan OAS

- Option Value = $V_{\text{no-pp}} - V_{\text{pp}}$.
- Option Adjusted Price (OAP) = Market Price + Option Value

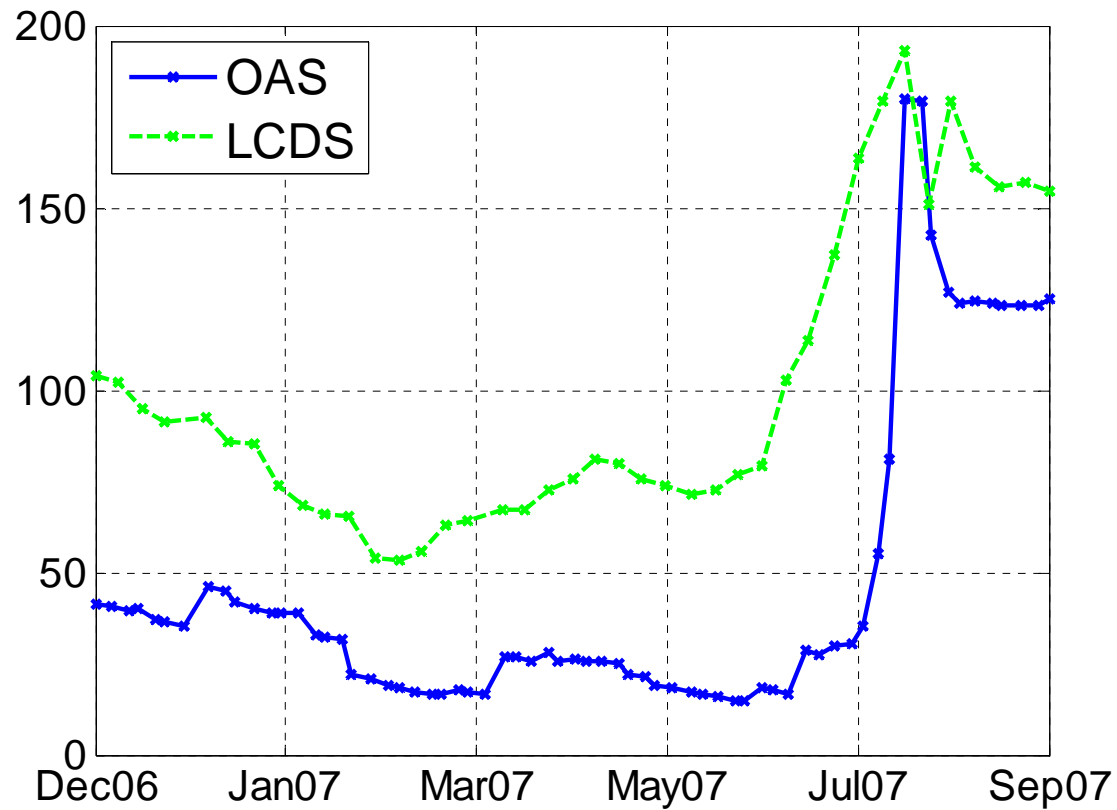
$$OAP = \sum_{i=1}^{T_M} \frac{CF_{t_i}}{(1 + r_{t_i}^{\text{risk-free}} + OAS)^{t_i}}$$

Option Value Example

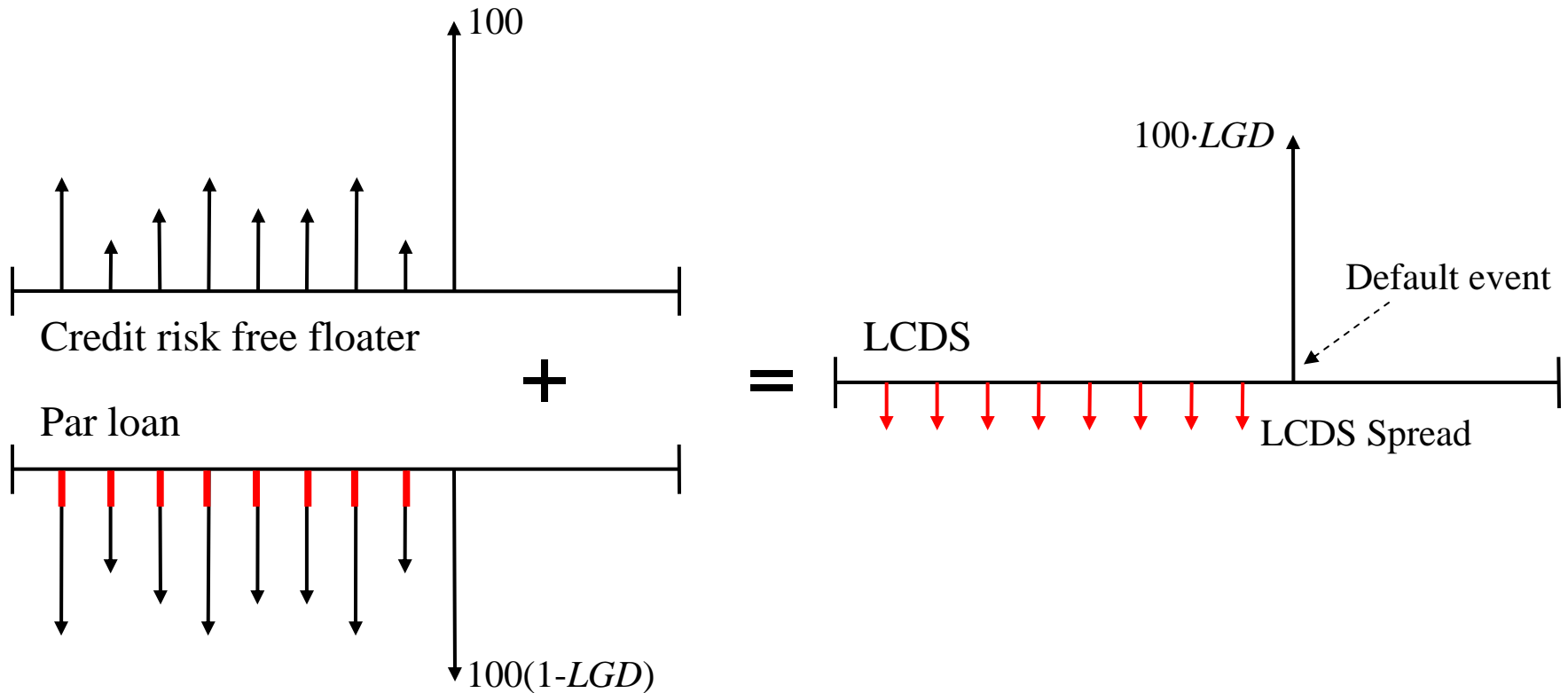
- Boyd Gaming Co, bullet term loan
- Originated 5/20/2004, 7yr tenor @ LIBOR+175bps
- Prepayment friction: no penalty, 100bps cost



Loan OAS vs LCDS Spread



Is loan OAS comparable to LCDS spread?

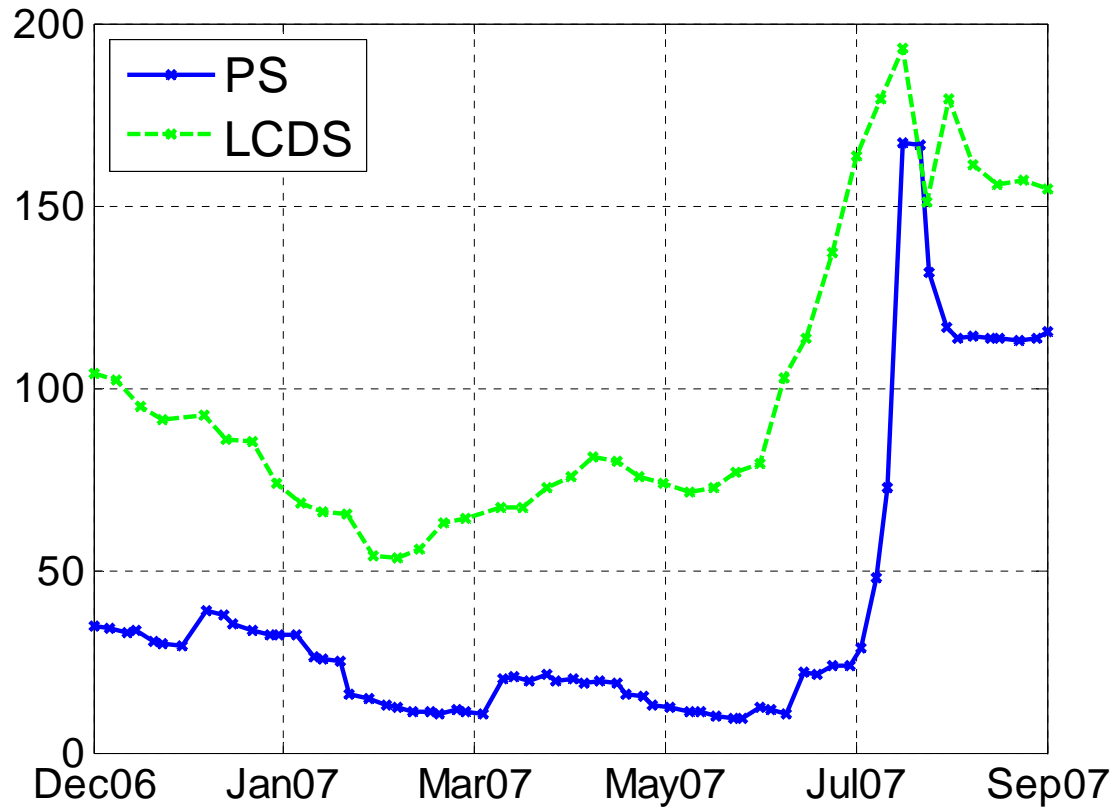


Loan Par Spread (PS)

- The par spread (PS) is defined to be the implied contractual spread of a (hypothetical) non-prepayable loan trading at par that has the same credit risk as the observed loan (same OAS).

$$1 = \sum_{i=1}^{t_{M-1}} \frac{\left(r_{t_{i-1}, t_i}^{\text{zero-EDF}} + PS \right) \cdot (t_i - t_{i-1})}{\left(1 + r_{t_i}^{\text{zero-EDF}} + OAS \right)^{t_i}} + \frac{1 + \left(r_{t_{M-1}, t_M}^{\text{zero-EDF}} + PS \right) \cdot (t_M - t_{M-1})}{\left(1 + r_{t_M}^{\text{zero-EDF}} + OAS \right)^{t_M}}$$

PS vs LCDS Spread

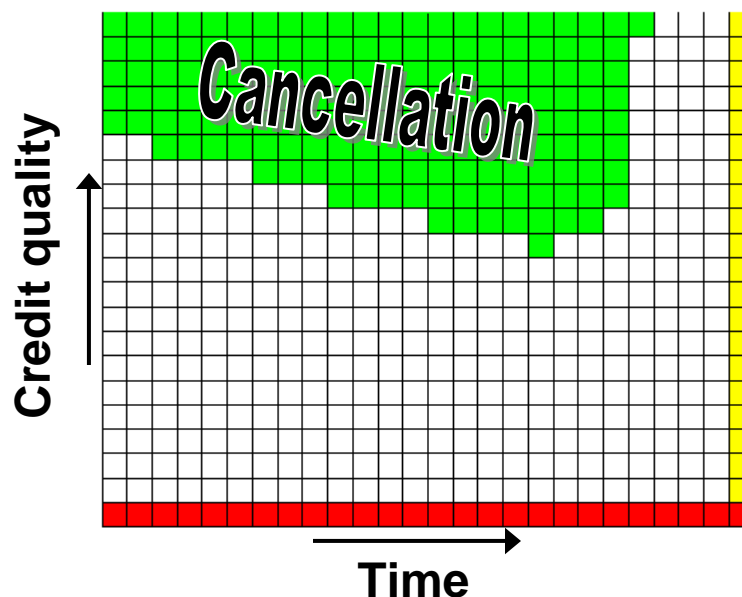


4

How Cancelable are LCDS Contracts?

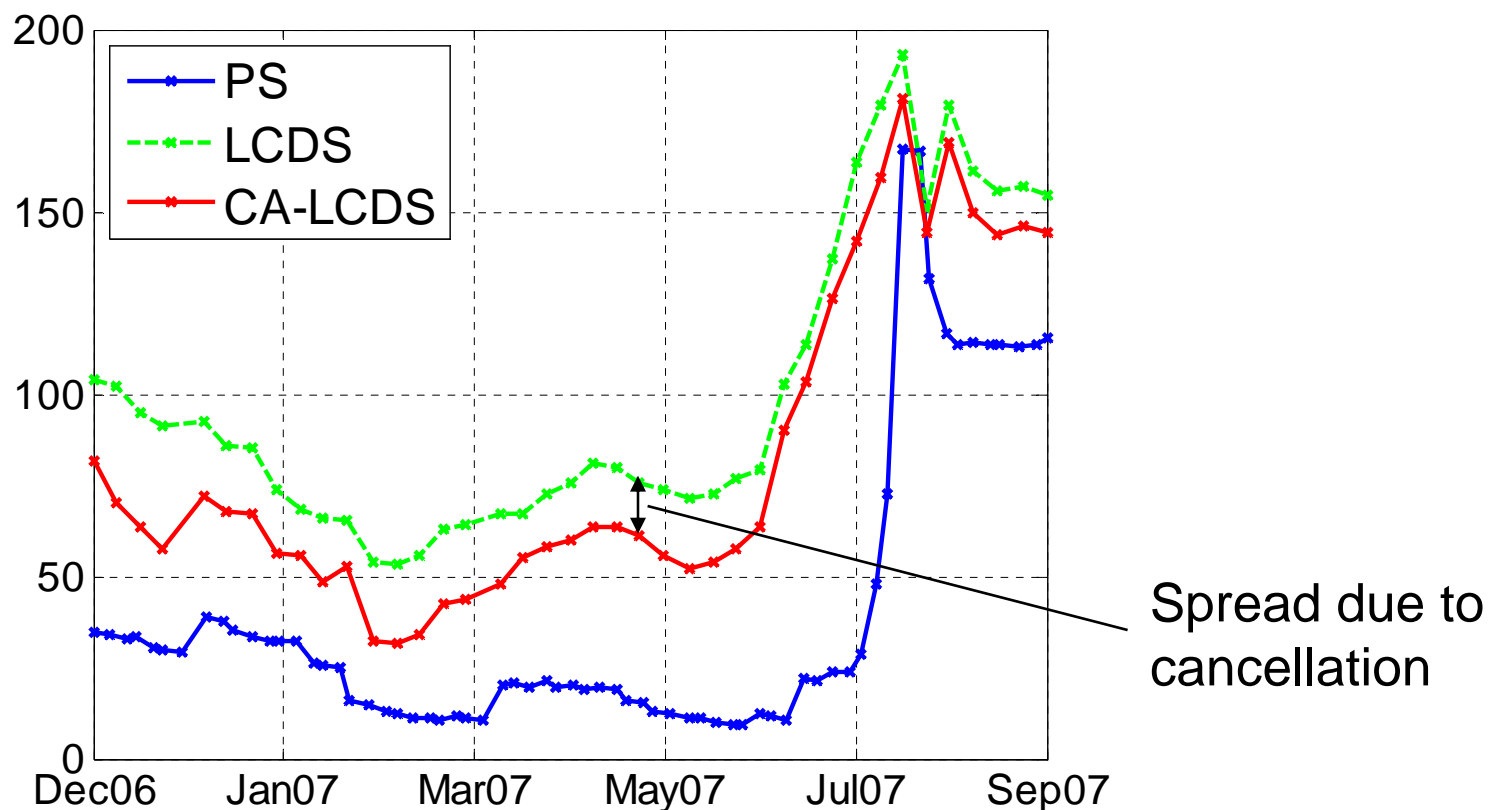
Modeling Pay-off of the Entire Loan Class

- An LCDS contract is cancelable when the entire class of underlying loans has extinguished.
- A likely scenario for LCDS cancellation to occur is when a borrower transitions from the (high-yield) loan market to the (investment-grade) bond market.
- We apply the lattice model to extract prepayment structure of a loan with an investment-grade contractual spread.



Cancellation-Adjusted LCDS

- We use the cancellation decision matrix to calculate the model LCDS spread with cancellation so that the dollar value is 0
- We can also calculate the par LCDS spread without cancellation



Spread due to cancellation

5

Duration and Convexity

Effective Spread and EDF Duration

$$D_{Spread} = -\frac{1}{V} \left(\frac{\partial V}{\partial S} \right) \qquad D_{EDF} = -\frac{1}{V} \left(\frac{\partial V}{\partial EDF} \right)$$

Spread and PD (EDF) PV01

$$PV01_{Spread} = - \left(\frac{\partial V}{\partial S} \right)$$

$$PV01_{EDF} = - \left(\frac{\partial V}{\partial EDF} \right)$$

Spread and EDF Convexity

$$C_{spread} = 0.5 \cdot \frac{1}{V} \left(\frac{\partial^2 V}{\partial S^2} \right)$$

$$C_{EDF} = 0.5 \cdot \frac{1}{V} \left(\frac{\partial^2 V}{\partial S^2} \right)$$

6

Summary

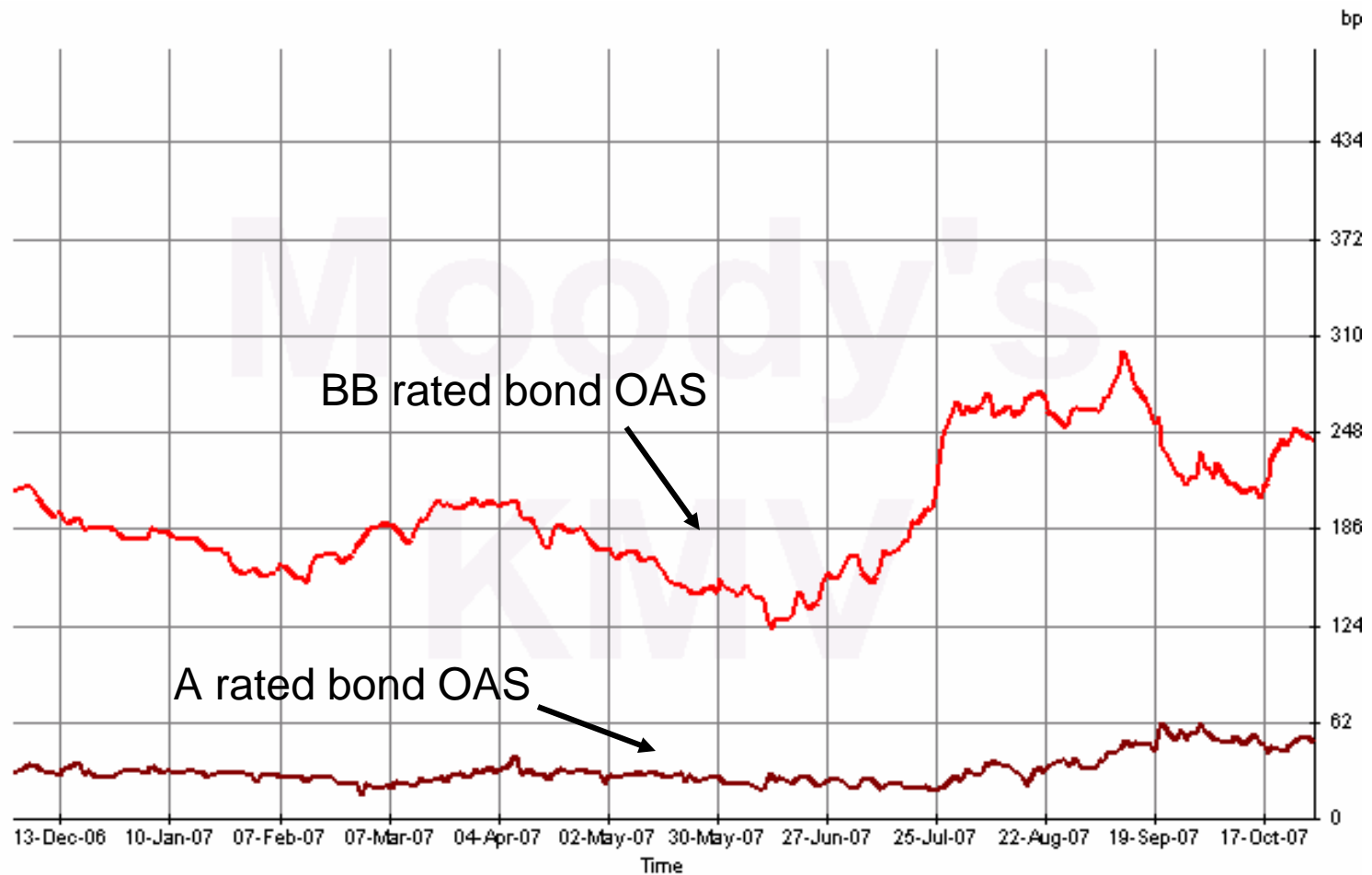
Summary

- Embedded options in loans and lattice valuation
- Prepayment patterns over time and early termination probability
- Expected life
- Option adjusted spread and par spread
- LCDS spread vs. OAS and par spread
- Cancellation options of LCDS

Boyd Gaming Co. Bond CDS Spreads



Investment-Grade vs. High-Yield Bond OAS



Source: Reuters EJV